

An important notion in Computer Science is the syntactical concept of terms. Examples of terms can be:

- $a$
- $b$
- $f(a, b)$
- $s(a)$
- $g(f(a, b), b, s(a))$

Sets of terms are usually defined by *induction*. In such a schema, a set of terms is seen in a constructive way: each element of an inductively defined set is either *constructed from* simpler elements of the set or a *basic* element. For instance,  $a$  is a basic element,  $g(f(a, b), b, s(a))$  is constructed from  $f(a, b)$ ,  $b$  and from  $s(a)$  using the constructor  $g$ . In the same vein,  $f(a, b)$  is constructed from  $a$  and from  $b$  using the constructor  $f$ .

More formally, an inductive definition of a set  $T$  of terms is composed by a non-empty set  $B$  of basic elements and a set  $K$  of constructors. Then, we say that  $T$  is the smallest set  $X$  containing  $B$  (i.e.  $B \subseteq X$ ) and the elements that respect the following rule:

let be  $f \in K$  with an arity of  $n$ , and let be  $n$  elements of  $X$  (say,  $a_1 \dots a_n$ ) then  
 $f(a_1, \dots, a_n)$  must be in  $X$

Let  $h_B : B \rightarrow \mathbb{N}$  be a total function that maps every symbol of  $B$  to a positive integer, and  $h_K$  be a total function over  $K$  that maps every  $n$ -ary constructor to an  $n$ -ary function over positive integers.

In such a setting, we define the notion of *natural interpretation*  $h$  as a function from  $T$  to  $\mathbb{N}$  that maps every term  $t \in T$  to a positive integer in the following way:

$$\begin{cases} h(a) & = h_B(a) \text{ if } a \in B \\ h(f(a_1 \dots a_n)) & = h_K(f)(h(a_1) \dots h(a_n)) \end{cases}$$

We say that an inductive definition  $T$  paired with a natural interpretation  $h$  is *ambiguous* when there exist two terms  $t_1, t_2 \in T$  such that  $h(t_1) = h(t_2)$ . We also say that  $(T, h)$  is *incomplete* when there exists a positive integer  $n$  such that there is no term  $t$  that verifies  $h(t) = n$ . Finally we say that  $(T, h)$  is *regular* if it is neither incomplete nor ambiguous.

Given an inductive definition of a set  $T$  of term and a natural interpretation  $h$ , your task consists in qualifying if  $(T, h)$  is ambiguous, incomplete, both or regular.

In the context of this problem, we will only consider simple interpretations. As a consequence, elements in  $h_K$  are simple functions defined by the following grammar:

$$f ::= (f + f) \mid (f * f) \mid \text{var}_{id} \mid \mathbb{N}$$

For a  $p$ -ary function, the only valid *var<sub>id</sub>* are  $x_1, x_2 \dots x_p$ ,  $x_1$  for the first argument,  $x_2$  for the second argument, and so on. Consider that every component in the definition of a function is separated from the other by a single space. For instance the *successor* function is described by  $(x_1 + 1)$ .

In order to simplify the problem, you will not have to consider the whole set of natural numbers. You only will have to consider the set  $\{N..M\}$  with  $0 \leq N < M \leq 30000$ , both provided by the input data. Consider also that each constructor have at least one parameter and at most 5 parameters.

## Input

**The input will contain several test cases, each of them as described below. Consecutive test cases are separated by a single blank line.**

The input consists in the following lines:

- the first line contains  $N$  and  $M$ , in this order and separated by a single space;
- the second line contains a single integer  $n$  ( $1 \leq n$ ) that represents the number of elements of  $B$ ;
- the next line contains a single integer  $m$  ( $0 \leq m$ ) that is the number of constructors;
- the following  $m$  lines introduce the arity of the  $m$  constructors. Thus, each line contains a single integer;
- the next  $n$  lines define the function  $h_B$ . The first of these lines contains an integer  $x$  ( $= h_B(a)$ ) related to the first basic element  $a$  (remember,  $N \leq x \leq M$ ). And so on;
- the last  $m$  lines define  $h_K$ . Each line is then the description of a function that respects the grammar exposed above.

## Output

**For each test case, the output must follow the description below. The outputs of two consecutive cases will be separated by a blank line.**

The output is organized following one of these four situations:

**Case  $(T, h)$  is regular:** a single line with the word 'REGULAR'.

**Case  $(T, h)$  is incomplete:** a single line with the word 'INCOMPLETE', a single space followed by a integer that is the smallest value that cause the incompleteness of  $(T, h)$ .

**Case  $(T, h)$  is ambiguous:** a single line with the word 'AMBIGUOUS', a single space followed by a integer that is the smallest value that turns  $(T, h)$  ambiguous.

**Case  $(T, h)$  is both incomplete and ambiguous:** the output is, in this case, two lines long. The first line reports the incompleteness along the lines of the second case. The second line reports the ambiguity of  $(T, h)$  in the same way as the third case.

## Sample Input

```
0 30000
1
1
1
0
(x1 + 1 )
```

```
0 30000
1
1
1
1
(x1 + 1 )
```

```
0 30000
1
2
1
2
1
(x1 + 1 )
(x1 + x2 )
```

## Sample Output

```
REGULAR
```

```
INCOMPLETE 0
```

```
INCOMPLETE 0
```

```
AMBIGUOUS 2
```