

An addition chain for  $n$  is an integer sequence  $\langle a_0, a_1, a_2, \dots, a_m \rangle$  with the following four properties:

- $a_0 = 1$
- $a_m = n$
- $a_0 < a_1 < a_2 < \dots < a_{m-1} < a_m$
- For each  $k$  ( $1 \leq k \leq m$ ) there exist two (not necessarily different) integers  $i$  and  $j$  ( $0 \leq i, j \leq k-1$ ) with  $a_k = a_i + a_j$

You are given an integer  $n$ . Your job is to construct an addition chain for  $n$  with minimal length. If there is more than one such sequence, any one is acceptable.

For example,  $\langle 1, 2, 3, 5 \rangle$  and  $\langle 1, 2, 4, 5 \rangle$  are both valid solutions when you are asked for an addition chain for 5.

## Input

The input file will contain one or more test cases. Each test case consists of one line containing one integer  $n$  ( $1 \leq n \leq 10000$ ). Input is terminated by a value of zero (0) for  $n$ .

## Output

For each test case, print one line containing the required integer sequence. Separate the numbers by one blank.

## Sample Input

```
5
7
12
15
77
0
```

## Sample Output

```
1 2 4 5
1 2 4 6 7
1 2 4 8 12
1 2 4 5 10 15
1 2 4 8 9 17 34 68 77
```