

## D: Dominoes Magic Squares

Source file name: dominoes.c, dominoes.cpp, dominoes.java, or dominoes.py

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A *domino set* is a collection of tiles of the form

$$[a \mid b]$$

with integer labels  $a$  and  $b$  satisfying  $0 \leq a, b \leq 6$ . Both  $[a \mid b]$  and  $[b \mid a]$  are descriptions of the same domino tile. A complete domino set has exactly 28 tiles and the sum of all its labels is 168.

A *magic square* is a square of integer numbers whose rows, columns, and diagonals have the same sum. Since domino tiles can be seen as planar objects of 2 unit squares, they can be used to build magic squares. For instance, the set of domino tiles

$$[1 \mid 4], [5 \mid 2], [4 \mid 4], [2 \mid 3], [5 \mid 4], [5 \mid 3], [1 \mid 3], [3 \mid 3]$$

can be arranged into a magic square of side 4 units with rows, columns, and diagonals adding up to 13:

4	4	2	3
3	3	2	5
1	3	5	4
5	3	4	1

However, it is impossible to build a  $4 \times 4$  magic square with the following set of tiles adding up to 15 in rows, columns, and diagonals:

$$[6 \mid 5], [2 \mid 4], [2 \mid 2], [5 \mid 5], [5 \mid 4], [5 \mid 1], [2 \mid 3], [3 \mid 6].$$

Assume you are given 8 domino tiles: can you arrange them into a  $4 \times 4$  magic square?

### Input

The input consists of several test cases. A test case comprises 8 consecutive lines of input, each one containing two blank-separated integers  $a$  and  $b$ ,  $0 \leq a, b \leq 6$ , representing the tile  $[a \mid b]$ . You can assume that a test case does not contain repeated dominoes.

*The input must be read from standard input.*

### Output

For each test case, output one line with the unique character 'Y' if a magic square can be built with the given domino tiles and 'N' otherwise.

*The output must be written to standard output.*

<b>Sample Input</b>	<b>Sample Output</b>
1 4	Y
5 2	N
4 4	
2 3	
5 4	
5 3	
1 3	
3 3	
6 5	
2 4	
2 2	
5 4	
5 5	
5 1	
2 3	
3 6	