Have you tried this horrible-looking puzzle?

- 1. Which question is the first question whose answer is b? (a) 2; (b) 3; (c) 4; (d) 5; (e) 6;
- 2. The only question that has the same answer as its next question is (e.g. option e means question 6 and 7's answers are the same): (a) 2; (b) 3; (c) 4; (d) 5; (e) 6;
- 3. Among the 5 options, which question has the same answer as this question (i.e. question 3)? (a) 1; (b) 2; (c) 4; (d) 7; (e) 6; 4. How many questions' answer is a? (a) 0; (b) 1; (c) 2; (d) 3; (e) 4
- 5. Which of the following questions has the same answer as this question? (a) 10; (b) 9; (c) 8; (d) 7; (e) 6;
- 6. The number of questions whose answer is a, equals the number of questions whose answer is: (a) b; (b) c; (c) d; (d) e; (e) none of above
- 7. What is the difference of this question's answer and the next question's answer (e.g. the difference of a and b is 1)? (a) 4; (b) 3; (c) 2; (d) 1; (e) 0;
- 8. How many questions' answer is a vowel? (only a and e are vowels. Others are consonants) (a) 2; (b) 3; (c) 4; (d) 5; (e) 6 9. The number of questions whose answer is a consonant is: (a) a prime; (b) a factorial; (c) a square
- number; (d) a cubic number; (e) a multiple of 5 10. The answer of this question is: (a) a; (b) b; (c) c; (d) d; (e) e;
- 1. make sure that your answer is not self-contradicting. For example, the first question's answer can't be b.

Note:

- (because no question is "the only question" that satisfying the condition) It's possible to solve this problem by hand, but as a programmer, solving it with a program is more
- How to Solve the Puzzle with a Program

Here's one way: enumerate all possible answers ( $5^{10} = 9765625$ ), and for each question, check

whether only your answer is correct. Pseudo-code: forall(answer\_list): bad = False

# your answer should be correct if testing\_option == answer\_list[testing\_question] and

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check(testing_question, testing_option) == True:
       bad = True
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if not bad: print answer\_list

if testing\_option != answer\_list[testing\_question] and

# other options must be incorrect

for testing\_question in [1,2,3,4,5,6,7,8,9,10]:

each answer, it is "1c2d3e4b5e6e7d8c9b10a") Amazing, huh? There's more. You wish that your program could solve some other puzzles, but first of all, you need to formulate the puzzle in a formal language.

Here "answer\_list" is a list of letters (subscript is 1-based), where the i-th letter is the answer to

Believe or not, the only answer is: "cdebeedcba" (if you prefer to add the question index before

This problem uses a LISP dialect to represent the puzzle. Don't worry if you don't know LISP, it has a very simple syntax. (f a b) means calling a function f with parameters a and b. That's like f(a, b) in C/C++/Java. Similarly, (f a (g b c) d) is like f(a, g(b, c), d) in C/C++/Java.

b. 2 c. 4

d. 7 e. 6

### is the expression presented in the option "c" of this question. Note that testing\_option's text can be a complex expression instead of a simple value. Refer to Sample Input.

represent boolean constants.

text below, 'iff' means "if and only if".

• Integers are always non-negative integers.

check(testing\\_question, testing\\_option):

result of testing\\_option of testing\\_question

lows:

- Here are the details of the LISP dialect used in this problem: • There are four datatypes: integer, string, boolean and functions.
- String literals are always enclosed by double quotes, like "a string". • There is no variable. All the so-called "identifiers" (consisting of letters and hyphens) are always pre-defined functions.

Below is a list of pre-defined functions. Functions starting with '!' means it may throw an exception, and functions starting with '@' means it can handle exceptions. Like C++/Java/Python, once an exception is raised, the evaluation process is stopped unless a function handles the exception. In the

tion idx. Also raises an exception on error.

Predicate is a special kind of function. It always takes a value of any type and returns a boolean

returns true iff the parameter is a single letter and is a vowel

returns true iff the parameter is a positive prime

return true iff a and b are of the same type and are equal. In this

Returns the "evaluation result" of option answer\_list[idx] of ques-

Return id of the first question that satisfies 'pred'. Raises an

returns a predicate (p v) which returns true iff (pred v) is false.

returns a predicate (p v) which returns true iff (pred1 v) and (pred2 v) are both true. Both pred1 and pred2 need to be

returns a predicate (p v) which returns true iff at least one of

(pred1 v) and (pred2 v) is true. Both pred1 and pred2 need to be evaluated. No short-circuit operation should be done.

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problem, you'll never need to compare two functions.

# !(answer-value idx)

value.

Predicates

Basic functions

(equal a b)

prime-p factorial-p

square-p

cubic-p vowel-p

Queries and statistics

consonant-p

Return id of the last question that satisfies 'pred'. Raises an !@(last-question pred) exception if not found. !@(only-question pred) Return id of the only question that satisfies 'pred'. Raises an exception if not found or more than one question found. @(count-question pred) Return the number of questions that satisfies 'pred'. !(diff-answer idx1 The difference of answers of question idx1 and idx2. exception on error, otherwise the return value is always  $0 \dots m-$ 1, where m is the number of options for each question.

Note that in the first four functions (those with a '@' flag), if an exception was raised when evaluating the predicate, the exception is handled and the predicate is not considered satisfied. For example, if answer\_list is "abc", (count-question (make-answer-diff-next-equal 0)) returns 0 and doesn't raise an exception, even though evaluating the predicate for question 3, i.e. ((make-answerdiff-next-equa 0) 3) raised an exception. However, all other functions will not handle exceptions. For example, if there

are only 3 questions, (factorial-p (answer-value 5)) will raise an exception instead of returning Predicate generators There are also functions that can create predicates on-the-fly: !(make-answer-diff-next- equal returns a predicate (p idx) which evaluates (diff-answer idx idx+1) and returns true if the result equals to num. Raises num) an exception if num is not an integer. (make-answer-equal a) returns a predicate (p idx) which evaluates (answer idx) and returns true if the result equals a.

### $2 \le m \le 5$ ), the number of questions and the number of options per question. Each question is described with m+1 lines: the question's expression and the options. Questions are numbered $1 \dots n$ , and options are labeled 'a'..'e'. Options are valid expressions and will not call option-value (calling optionvalue makes it recursive!). Each question is followed by a blank line. Most test cases are easy.

Input

"b"

3 2

(make-not pred)

(make-and pred1 pred2)

(make-or pred1 pred2)

(equal (option-value) (answer 2)) "none-of-above" (equal (option-value) (first-question (make-answer-diff-next-equal 0)))

## ((option-value) (diff-answer 1 2)) factorial-p

(make-not square-p) (make-not cubic-p) "none-of-above"

"none-of-above'

bcb cca

aab

ba

 ${\tt prime-p}$ 

(make-is-multiple 2)

(make-not (make-is-multiple 2))

(equal (option-value) (answer 1))

(equal (only-question (option-value)) 1)

(make-answer-is consonant-p) (make-answer-is vowel-p) (make-answer-value-equal 1) (make-answer-value-is square-p)
"none-of-above" (option-value)

((option-value) (last-question (make-answer-equal "b")))

((option-value) (last-question (make-answer-diff-next-equal 0)))

Case 1: Case 2:

Case 3: aba Case 4: ab ee Case 5:

Sample Output

2. make sure that for each question, only your answer is correct, all other options must be incorrect. For example, if your answer to question 5 is a, then none of question 9, 8, 7, 6's answers can be a! 3. make sure that your answer won't make any question invalid. For example, if question 2 and 3's answer are the same, and question 8,9's answers are also the same, question 2 would be invalid

for testing\_option in ["a","b","c","d","e"]: check(testing\_question, testing\_option) == False: bad = True

Here is an example of how to describe a question of the puzzle: 3. (equal (answer 3) (answer (option-value)))

Formalizing the Puzzle

There are two very important built-in functions involved:  $\underline{returns} \underline{answer\_list[idx]}$  in the pseudo-code above. (answer idx) returns the "evaluation result" of testing\_option's text, treated as (option-value) an expression.

In the example above, if testing\_option is "c", then (option-value) returns 4 (an integer) because 4

The function "check(testing\_question, testing\_option)" above can be implemented as fol-

There is one special option expression: "none-of-above". The result of "none-of-above" depends on other options' evaluation results. In this problem, there can be at most one "none-of-above" for each

• There are only two boolean values: true and false. Note that there are no "boolean literal", so you don't care whether to use #t and #f (like in Scheme), or t and nil (like in Common Lisp) to

question, and it must be the last option. Details

1. set-up the function (option-value) so that it returns the evaluation

(equal (answer 3) (answer (option-value))) in the example above)

2. evaluate the lisp expression of testing  $\q$ question (e.g. the expression

3. if an unhandled exception is raised during the evaluation, returns False 4. if the result of step 2 is boolean, return it; otherwise return False

(option-value) iscussed above. !(answer idx) discussed above. If idx is not an integer or is not in  $1 \dots n$  (where n is the number of questions), then raises an exception

self-explanatory

self-explanatory self-explanatory

self-explanatory

!@(first-question pred) exception if not found.

returns a predicate (p idx) which evaluates (answer idx) and (make-answer-is pred) returns true if the result satisfies 'pred'. self-explanatory. The predicate evaluates (answer-value idx) (make-answer-value-equal a) (make-answer-value-is pred) self-explanatory. The predicate evaluates (answer-value idx) returns a predicate (p i) which returns true iff i is an integer !(make-is-multiple num) and is a multiple of num. Raises an exception if num is not an integer. !(make-equal val) returns a predicate (p v) which returns true iff (equal v val) is true. Raises an exception if val is neither an integer nor a

For example, (make-is-multiple 3) returns a predicate "is a multiple of 3", so ((make-is-multiple 3) 6) returns true and ((make-is-multiple 3) 10) returns false. Similarly (make-not (make-or

There will be at most 50 test cases. Each test case begins with two integers n and m ( $2 \le n \le 10$ ,

square-p prime-p)) returns a predicate "neither a square nor a prime".

Output For each test case, print the case number in the first line, and a list of answers, one per line, sorted in ascending order. There will always be at least one answer. Note: This problem is complex. If you have any questions, email me: rujia.liu@gmail.com Sample Input (equal (option-value) (count-question (make-answer-equal "a"))) (equal (option-value) "a") ((option-value) (count-question (make-answer-equal "c")))
(make-and (make-is-multiple 2) (make-or factorial-p prime-p)) (make-not prime-p) "none-of-above"

(make-equal 2) ((option-value) (only-question (make-answer-equal "b"))) (make-is-multiple 2) "none-of-above

(equal (first-question (make-answer-diffnext-equal 2)) (first-question (makeanswer-diff-next-equal 2))) (equal (option-value) 1)