You have a grid of $n$ rows and $n$ columns. Each of the unit squares contains a non-zero digit. You walk from the top-left square to the bottom-right square. Each step, you can move left, right, up or down to the adjacent square (you cannot move diagonally), but you cannot visit a square more than once. There is another interesting rule: your path must be symmetric about the line connecting the bottom-left square and top-right square. Below is a symmetric path in a $6 \times 6$ grid.


Your task is to find out, among all valid paths, how many of them have the minimal sum of digits?

## Input

There will be at most 25 test cases. Each test case begins with an integer $n(2 \leq n \leq 100)$. Each of the next $n$ lines contains $n$ non-zero digits (i.e. one of $1,2,3, \ldots, 9$ ). These $n^{2}$ integers are the digits in the grid. The input is terminated by a test case with $n=0$, you should not process it.

## Output

For each test case, print the number of optimal symmetric paths, modulo $1,000,000,009$.

## Sample Input

2
11
11
3
111
111
211
0

## Sample Output

2

