

## 11317 GCD + LCM

Given the value of  $N$ , you will have to find the number of digits in  $G$  and  $L$  in base googol ( $10^{100}$ ). The definition of  $G$  and  $L$  are given below:

$$G = \prod_{i=1}^{N-1} \prod_{j=i+1}^N GCD(i, j) \quad L = \prod_{i=1}^{N-1} \prod_{j=i+1}^N LCM(i, j)$$

If you are not accustomed with the symbol  $\prod$ , then for your kind information we give an example:

$$\prod_{i=1}^{4-1} \prod_{j=i+1}^4 GCD(i, j) = GCD(1, 2) * GCD(1, 3) * GCD(1, 4) * GCD(2, 3) * GCD(2, 4) * GCD(3, 4)$$

Here  $GCD(i, j)$  means the greatest common divisor of integer  $i$  and integer  $j$ , and  $LCM(i, j)$  means the Least Common Multiplicand of integer  $i$  and integer  $j$ .

### Input

The input file contains at most 100 lines of inputs. Each line contains an integer  $N$  ( $1 < N < 1000001$ ). Input is terminated by a line containing a single zero.

### Output

For each line of input produce one line of output. This line contains the serial of output followed by two integers  $DG$  and  $DL$ . Here  $DG$  is the number of digits in  $G$  when written in base googol and  $DL$  is the number of digits in  $L$  when written in base googol. Don't even think of submitting a brute force solution: It will probably take more than 2 years for the largest possible input. Look at the output for sample input for format details.

### Sample Input

```
10
100
20000
0
```

### Sample Output

```
Case 1: 1 1
Case 2: 11 146
Case 3: 494294 14972385
```