

## 10302 Summation of Polynomials

The following text was taken from a book of mathematics:

“The antidifference of a function  $f(x)$  is the function  $g(x)$  such that  $f(x) = g(x + 1) - g(x)$ . So, if we have a summation of  $f(x)$ , it can be simplified by the use of its antidifference in the following way:

$$\begin{aligned} f(k) + f(k + 1) + f(k + 2) + \dots + f(k + n) &= \\ = g(k + 1) - g(k) + g(k + 2) - g(k + 1) + g(k + 3) - g(k + 2) + \dots + g(k + n + 1) - g(k + n) &= \\ &= g(k + n + 1) - g(k) \end{aligned}$$

A factorial polynomial is expressed as  $k^{\{n\}}$  meaning the following expression:

$$k * (k - 1) * (k - 2) * \dots * (k - (n - 1))$$

The antidifference of a factorial polynomial  $k^{\{n\}}$  is  $k^{\{n+1\}}/(n + 1)$ .”

So, if you want to calculate  $S_n = p(1) + p(2) + p(3) + \dots + p(n)$ , where  $p(i)$  is a polynomial of degree  $k$ , we can express  $p(i)$  as a sum of various factorial polynomials and then, find out the antidifference  $P(i)$ . So, we have  $S_n = P(n + 1) - P(1)$ .

### Example:

$$S = 2 * 3 + 3 * 5 + 4 * 7 + 5 * 9 + 6 * 11 + \dots + (n + 1) * (2n + 1) = p(1) + p(2) + p(3) + p(4) + p(5) + \dots + p(n),$$

where  $p(i) = (i + 1)(2i + 1)$ .

Expressing  $p(i)$  as a factorial polynomial, we have:

$$p(i) = 2i^{\{2\}} + 5i + 1.$$

and then

$$P(i) = (2/3)i^{\{3\}} + (5/2)i^{\{2\}} + i.$$

Calculating  $P(n + 1) - P(1)$  we have

$$S = (n/6) * (4n^2 + 15n + 17)$$

Given a number  $1 \leq x \leq 50,000$ , one per line of input, calculate the following summation:

$$1 + 8 + 27 + \dots + x^3$$

### Input

Input file contains several lines of input. Each line contain a single number which denotes the value of  $x$ . Input is terminated by end of file.

### Output

For each line of input produce one line of output which is the desired summation value.

**Sample Input**

1  
2  
3

**Sample Output**

1  
9  
36