In 1883, Edward Lucas invented, or perhaps reinvented, one of the most popular puzzles of all times – the Tower of Hanoi, as he called it – which is still used today in many computer science textbooks to demonstrate how to write a recursive algorithm or program. First of all, we will make a list of the rules of the puzzle:

- $\bullet\,$  There are three pegs:  $A,\,B$  and C.
- There are n disks. The number n is constant while working the puzzle.
- All disks are different in size.
- The disks are initially stacked on peg A so that they increase in size from the top to the bottom.
- The goal of the puzzle is to transfer the entire tower from the  $\tt A$  peg to the peg  $\tt C.$
- One disk at a time can be moved from the top of a stack either to an empty peg or to a peg with a larger disk than itself on the top of its stack.

Your job will be to write a program which will show a copy of the puzzle on the screen step by step, as you move the disks around. This program has to solve the problem in an efficient way.

**TIP:** It is well known and rather easy to prove that the minimum number of moves needed to complete the puzzle with n disks is  $2^n - 1$ .

## Input

The input file will consist of a series of lines. Each line will contain two integers n, m. n, lying within the range [1, 250], will denote the number of disks and m, belonging to  $[0, 2^n - 1]$ , will be the number of the last move, you may assume that m will also be less than  $2^{16}$ , and you may also assume that a good algorithm will always have enough time. The file will end at a line formed by two zeros.

# Output

The output will consist again of a series of lines, formatted as show below.

## NOTES:

- There are 3 spaces between de '=>' and the first number printed. If there isn't any number, there should be no spaces.
- All the disks in a single peg are printed in a single line (not as in the Problem #1 below).
- Print a blank line after every problem.

### Sample Input

# Sample Output

#### Problem #1

 $64 \ \ 63 \ \ 62 \ \ 61 \ \ 60 \ \ 59 \ \ 58 \ \ 57 \ \ 56 \ \ 55 \ \ 54 \ \ 53 \ \ 52 \ \ 51 \ \ 50 \ \ 49 \ \ 48 \ \ 47 \ \ 46 \ \ 45 \ \ 44 \ \ 43 \ \ 42 \ \ 41$ A=> 40 39 38 37 36 35 34 33 32 31 30 29 28 27 26 25 24 23 22 21 20 19 18 17 16 15 14 13 12 11 10 9 8 7 6 5 4 3 2 1 B=> C=>  $64 \ \ 63 \ \ 62 \ \ 61 \ \ 60 \ \ 59 \ \ 58 \ \ 57 \ \ 56 \ \ 55 \ \ 54 \ \ 53 \ \ 52 \ \ 51 \ \ 50 \ \ 49 \ \ 48 \ \ 47 \ \ 46 \ \ 45 \ \ 44 \ \ 43 \ \ 42 \ \ 41$ A=> 40 39 38 37 36 35 34 33 32 31 30 29 28 27 26 25 24 23 22 21 20 19 18 17 16 15 14 13 12 11 10 9 8 7 6 5 4 3 2 B=> 1 C=> A=>  $64 \ \ 63 \ \ 62 \ \ 61 \ \ 60 \ \ 59 \ \ 58 \ \ 57 \ \ 56 \ \ 55 \ \ 54 \ \ 53 \ \ 52 \ \ 51 \ \ 50 \ \ 49 \ \ 48 \ \ 47 \ \ 46 \ \ 45 \ \ 44 \ \ 43 \ \ 42 \ \ 41$ 40 39 38 37 36 35 34 33 32 31 30 29 28 27 26 25 24 23 22 21 20 19 18 17 16 15 14 13 12 11 10 9 8 7 6 5 4 3 B=> 1 C=> 2 Problem #2 87654321 A=> B=>

C=>

8765432 A=> B=> 1 C =>876543 A =>B=> 1 C =>2 876543 A =>B=> 2 1 C =>87654 A =>B=> З 2 1 C=> 876541 A =>B=> 3 C =>2 876541 A =>B=> 32 C =>87654 A =>321 B=> C =>8765 A =>321 B=> C =>4 A =>8765 32 B=> C=> 4 1 87652 A =>B=> 3 C =>4 1 876521 A =>B=> 3 C=> 4 A=> 876521 B=> 4 3 C=> A=> 87652 B=> 1 4 3 C =>A=> 8765 B=> 1 C=> 4 3 2 8765 A =>B=> C=> 4 3 2 1 A =>876 B=> 5 C =>4 3 2 1 A = >8761 B=> 5 4 3 2 C =>A=> 8761 B=> 52 43 C =>A =>876 B=> 521 C =>4 3

A=> B=> C=>	8 5 4	7 2	6 1	3			
A=> B=> C=>	8 5 4	7 2 1	6	3			
A=> B=> C=>	8 5 4	7	6	3	2		
A=> B=> C=>	8 5 4	7	6	3	2	1	
A=> B=> C=>	8 5	7 4	6	3	2	1	
A=> B=> C=>	8 5	7 4	6 1	3	2		
A=> B=> C=>	8 5 2	7 4	6 1	3			
A=> B=> C=>	8 5 2	7 4 1	6	3			
A=> B=> C=>	8 5 2	7 4 1	6 3				
A=> B=> C=>	8 5 2	7 4	6 3	1			
A=> B=> C=>	8 5	7 4	6 3	1 2			
A=> B=> C=>	8 5	7 4	6 3	2	1		
A=> B=> C=>	8 5 6	7 4	3	2	1		
A=> B=> C=>	8 5 6	7 4 1	3	2			
A=> B=> C=>	8 5 6	7 4 1	2 3				
A=> B=> C=>	8 5 6	7 4	2 3	1			
A=> B=> C=>	8 5 6	7 4 3	2	1			
A=> B=> C=>	8 5 6	7 4 3	2 1				
A=> B=> C=>	8 5 6	7 4 3	1 2				

87 A=> B=> 54 C=> 6321 874 A =>B=> 5 6321 C=> 8741 A=> B=> 5 632 C=> 8741 A=> B=> 52 C=> 63 874 A=> 521 B=> C=> 63 A=> 8743 B=> 521 C=> 6 8743 A=> B=> 52 C=> 6 1