

## 115 Climbing Trees

Expression trees, B and B\* trees, red-black trees, quad trees, PQ trees; trees play a significant role in many domains of computer science. Sometimes the name of a problem may indicate that trees are used when they are not, as in the Artificial Intelligence planning problem traditionally called the *Monkey and Bananas problem*. Sometimes trees may be used in a problem whose name gives no indication that trees are involved, as in the *Huffman code*.

This problem involves determining how pairs of people who may be part of a “family tree” are related.

Given a sequence of *child-parent* pairs, where a pair consists of the child’s name followed by the (single) parent’s name, and a list of query pairs also expressed as two names, you are to write a program to determine whether the query pairs are related. If the names comprising a query pair are related the program should determine what the relationship is. Consider academic advisees and advisors as exemplars of such a single parent genealogy (we assume a single advisor, i.e., no co-advisors).

In this problem the child-parent pair  $p q$  denotes that  $p$  is the child of  $q$ . In determining relationships between names we use the following definitions:

- $p$  is a  $0$ -descendent of  $q$  (respectively  $0$ -ancestor) if and only if the child-parent pair  $p q$  (respectively  $q p$ ) appears in the input sequence of child-parent pairs.
- $p$  is a  $k$ -descendent of  $q$  (respectively  $k$ -ancestor) if and only if the child-parent pair  $p r$  (respectively  $q r$ ) appears in the input sequence and  $r$  is a  $(k - 1)$ -descendent of  $q$  (respectively  $p$  is a  $(k - 1)$ -ancestor of  $r$ ).

For the purposes of this problem the relationship between a person  $p$  and a person  $q$  is expressed as exactly one of the following four relations:

1. child — grand child, great grand child, great great grand child, *etc.*

By definition  $p$  is the “child” of  $q$  if and only if the pair  $p q$  appears in the input sequence of child-parent pairs (i.e.,  $p$  is a 0-descendent of  $q$ );  $p$  is the “grand child” of  $q$  if and only if  $p$  is a 1-descendent of  $q$ ; and

$p$  is the “great great . . . great grand child” of  $q$   
 $n$  times

if and only if  $p$  is an  $(n + 1)$ -descendent of  $q$ .

2. parent — grand parent, great grand parent, great great grand parent, *etc.*

By definition  $p$  is the “parent” of  $q$  if and only if the pair  $q p$  appears in the input sequence of child-parent pairs (i.e.,  $p$  is a 0-ancestor of  $q$ );  $p$  is the “grand parent” of  $q$  if and only if  $p$  is a 1-ancestor of  $q$ ; and

$p$  is the “great great . . . great grand parent” of  $q$   
 $n$  times

if and only if  $p$  is an  $(n + 1)$ -ancestor of  $q$ .

3. cousin — 0-th cousin, 1-st cousin, 2-nd cousin, *etc.*; cousins may be once removed, twice removed, three times removed, *etc.*

By definition  $p$  and  $q$  are “cousins” if and only if they are related (i.e., there is a path from  $p$  to  $q$  in the implicit undirected parent-child tree). Let  $r$  represent the least common ancestor of  $p$  and  $q$  (i.e., no descendent of  $r$  is an ancestor of both  $p$  and  $q$ ), where  $p$  is an  $m$ -descendent of  $r$  and  $q$  is an  $n$ -descendent of  $r$ .

Then, by definition, cousins  $p$  and  $q$  are “ $k$ -th cousins” if and only if  $k = \min(n, m)$ , and, also by definition,  $p$  and  $q$  are “cousins removed  $j$  times” if and only if  $j = |n - m|$ .

4. sibling — 0-th cousins removed 0 times are “siblings” (they have the same parent).

## Input

The input consists of child-parent pairs of names, one pair per line. Each name in a pair consists of lower-case alphabetic characters or periods (used to separate first and last names, for example). Child names are separated from parent names by one or more spaces. Child-parent pairs are terminated by a pair whose first component is the string ‘no.child’. Such a pair is NOT to be considered as a child-parent pair, but only as a delimiter to separate the child-parent pairs from the query pairs. There will be no circular relationships, i.e., no name  $p$  can be *both* an ancestor and a descendent of the same name  $q$ .

The child-parent pairs are followed by a sequence of query pairs in the same format as the child-parent pairs, i.e., each name in a query pair is a sequence of lower-case alphabetic characters and periods, and names are separated by one or more spaces. Query pairs are terminated by end-of-file.

There will be a maximum of 300 different names overall (child-parent and query pairs). All names will be fewer than 31 characters in length. There will be no more than 100 query pairs.

## Output

For each query-pair  $p$   $q$  of names the output should indicate the relationship  $p$  *is-the-relative-of*  $q$  by the appropriate string of the form

- child, grand child, great grand child, great great ... great grand child
- parent, grand parent, great grand parent, great great ... great grand parent
- sibling
- $n$  cousin removed  $m$
- no relation

If an  $m$ -cousin is removed 0 times then only ‘ $m$  cousin’ should be printed, i.e., ‘removed 0’ should NOT be printed. Do not print *st*, *nd*, *rd*, *th* after the numbers.

## Sample Input

```
alonzo.church oswald.veblen
stephen.kleene alonzo.church
dana.scott alonzo.church
martin.davis alonzo.church
pat.fischer hartley.rogers
mike.paterson david.park
dennis.ritchie pat.fischer
```

```
hartley.rogers alonzo.church
les.valiant mike.paterson
bob.constable stephen.kleene
david.park hartley.rogers
no.child no.parent
stephen.kleene bob.constable
hartley.rogers stephen.kleene
les.valiant alonzo.church
les.valiant dennis.ritchie
dennis.ritchie les.valiant
pat.fischer michael.rabin
```

### Sample Output

```
parent
sibling
great great grand child
1 cousin removed 1
1 cousin removed 1
no relation
```