



Jumping Frogs II

Input: Standard Input
Output: Standard Output



At time 0, F frogs are sitting on a straight line. All the positions of the frogs are non-negative integer numbers. Every second, all the frogs jump. Each of the frogs has its own velocity, i.e., every second the i^{th} frog jumps V_i units. Every frog jumps to its right.

The line is divided into $N + 1$ contiguous segment. The left end of the first segment is always 0 and the right end of the $(N+1)^{\text{th}}$ segment is 10^9 . The segments are denoted by a sequence of N positive integers, the right end point of first N segments. Every segment except the first one starts from the first point after the right endpoint of the last segment.

For example, if $N = 1$ and the sequence has 1 integer number 10, then there are two segments, one is from 0 to 10 and another is from 11 to 10^9 , both inclusive.

You are given the initial positions of all the F frogs and a sequence of positive integers describing the segments. Find the minimum time it will take all the frogs to reach a single segment. A frog is said to be on a segment if and only if it's sitting on some points inside the segment (including the endpoints). Please note that a frog is not said to be inside a segment when it's jumping.

Input

Input starts with a single positive integer, $1 \leq T \leq 10$, on a single line, denoting the number of test cases. Each of the following T test cases has the following 5 lines,

1. Blank line. To separate cases.
2. Two non-negative positive integers $1 \leq F \leq 1000$, $1 \leq N \leq 100,000$.
3. F non negative integers, where the i^{th} integer represents the position of the i^{th} frog.
4. F non negative integers, where the i^{th} integer represents the velocity of the i^{th} frog.
5. A sequence of N positive integers describing the segments.

Note that, all the numbers in the input are greater than 0 and less than 10^9 where a limit is not specified.

Output

For each case, print the minimum time it takes all the frogs to reach a single segment. If it's impossible for all the frogs to be on a single segment, print -1. For every case print the output on a single line.

Sample Input

```
2
1 1
10
10000
1000000
2 1
1 200
199 100
100
```

Output for Sample Input

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Case 1: 0
Case 2: 1
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Special Thanks: Hasnain Heickal