

NATIONAL COLLEGIATE PROGRAMMING CONTEST 2015 Department of Computer Science & Engineering Rajshahi University of Engineering & Technology

Kazla, Rajshahi-6204



# С

## Farey Sequence

The Farey sequence of order n is the sequence of completely reduced fractions between 0 and 1 which, when in lowest terms, have denominators less than or equal to n, arranged in ascending order. Farey sequence for different values of n are shown in the figure on the left below:

$$F_{1} = \left\{ \frac{0}{1}, \frac{1}{1} \right\}$$

$$F_{4} = \left\{ \frac{0}{1}, \frac{1}{4}, \frac{1}{3}, \frac{1}{2}, \frac{2}{3}, \frac{3}{4}, \frac{1}{1} \right\}$$

$$F_{7} = \left\{ \frac{0}{1}, \frac{1}{7}, \frac{1}{6}, \frac{1}{5}, \frac{1}{4}, \frac{2}{7}, \frac{1}{3}, \frac{2}{5}, \frac{3}{7}, \frac{1}{2}, \frac{4}{7}, \frac{3}{5}, \frac{2}{3}, \frac{5}{7}, \frac{3}{4}, \frac{4}{5}, \frac{5}{6}, \frac{6}{7}, \frac{1}{1} \right\}$$
Figure 1:

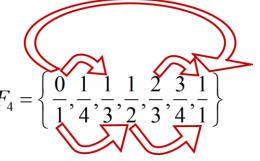


Figure 2: Five desired pairs in F<sub>4</sub>

It is very well known that if  $\frac{m_1}{n_1}$  and  $\frac{m_2}{n_2}$  are two consecutive fractions of a Farey Sequence then  $m_2n_1 - m_1n_2 = 1$ . But many fractions which are not consecutive also show this property. For example, in F<sub>7</sub>,  $\frac{2}{5}$  and  $\frac{1}{2}$  also show this property although they are not consecutive fractions in F<sub>7</sub>. Given the value of n, your job is to find number of pair of non-consecutive fractions  $\frac{m_i}{n_i}$ and  $\frac{m_j}{n_i}$ , such that  $m_jn_i - m_in_j = 1$ .

### Input

Input file contains at most 20000 lines of input. Each line contains a positive integer which denotes the value of n ( $0 \le n \le 1000001$ ). Input is terminated by a line containing a single zero. This line should not be processed.

### Output

For each line of input produce one line of output. This line contains number of pair of non-

consecutive fractions  $\frac{m_i}{n_i}$  and  $\frac{m_j}{n_j}$ , (j - i > 1) in Farey Series F<sub>n</sub>, such that  $m_j n_i - m_i n_j = 1$ 



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Sample Input	Output for Sample Input
1	0
4	5
0	

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