

# Problem J

## Lazy Professor

Source file name: `lazyprof.c`, `lazyprof.cpp` or `lazyprof.java`

Professor Yzal does not like to grade the exams of his students, so that he assigns this task to his assistants. Final students' grades are defined as weighted sums of the grades obtained in the exams. But Professor Yzal does not define *a priori* the exam's relative weights. Instead of that, only when the assistants end their job (and all the students' grades in each exam are known) Professor Yzal decides the exam's weights. He does it trying to be pleasant with the whole class, so that the assigned weights should maximize the average final grade that the class obtains, and expecting that eventual complaints about his grading criteria will be as few as possible. And finally, maybe rewarding harder exams, Yzal defines that the weight of every particular exam should lie within a specific range of values.

This term is about to finish and you were hired to help Yzal with his lazy grading job. Your task is to write a program that, given the students' grades and the *reasonable range* of weights for each exam, determines the maximum possible average according to the following rules:

- Each exam must have a weight, defined as an integer number in the closed interval  $[0, 100]$ , describing the assigned percentage.
- The weight of an exam  $i$  must be in an integer closed interval  $[min_i, max_i]$  that describes the corresponding reasonable range previously defined by Yzal.
- The sum of all exam weights must be 100.
- The final grade of each student is a weighted sum calculated as the sum of his/her own grades previously multiplied by the corresponding exam weight divided by 100.
- The exam weights are so chosen that the average of the students' final grades is maximized.

## Input

There are several cases to consider. Each test case is described as follows:

- A line with two integer numbers  $S$  and  $N$ , separated by a blank, ( $1 \leq S \leq 100$ ,  $1 \leq N \leq 20$ ), where  $S$  corresponds to the number of students and  $N$  corresponds to the number of exams in the course.
- Each one of the following  $S$  lines describes the grades of each student, containing  $N$  integer numbers  $c_{j1}, c_{j2}, \dots, c_{jN}$ , separated by a blank, ( $0 \leq c_{ji} \leq 100$  for each  $1 \leq i \leq N$ ), where  $c_{ji}$  indicates the grade obtained by the student  $j$  in the exam  $i$  ( $1 \leq j \leq S$ ,  $1 \leq i \leq N$ ).
- Each one of the following  $N$  lines describes the reasonable range of weights of each exam, containing two integer numbers  $min_i, max_i$ , separated by a blank ( $0 \leq min_i \leq max_i \leq 100$ ), where  $min_i$  and  $max_i$  represent the minimum and maximum weight that can be assigned to the exam  $i$ , respectively ( $1 \leq i \leq N$ ).

You can suppose that

$$\sum_{i=1}^N \min_i \leq 100, \quad \text{and} \quad \sum_{i=1}^N \max_i \geq 100.$$

The last test case is followed by a line containing two zeros.

*The input must be read from the file lazyprof.in.*

## Output

For each given case, output a single line with a number indicating the maximum possible average of the students' final grades if the weights are defined according to the rules. The answer should be formatted and approximated to two decimal places. The floating point delimiter must be '.' (i.e., the dot). The rounding applies towards the *nearest neighbor* unless both neighbors are equidistant, in which case the result is rounded up (e.g., 78.312 is rounded to 78.31; 78.566 is rounded to 78.57; 78.345 is rounded to 78.35, etc.).

*The output must be written to standard output.*

Sample input	Output for the sample input
1 1	0.00
0	70.00
0 100	67.00
2 2	65.00
50 90	72.90
70 50	
0 100	
0 100	
2 2	
50 90	
70 50	
30 70	
30 70	
2 2	
50 90	
70 50	
50 50	
50 50	
2 2	
73 52	
92 81	
20 50	
60 80	
0 0	