

Farey Polygon

In mathematics, the Farey sequence of order n is the sequence of completely reduced fractions between 0 and 1 which, when in lowest terms, have denominators less than or equal to n , arranged in order of increasing size. Each Farey sequence starts with the value 0, denoted by the fraction $0/1$, and ends with the value 1, denoted by the fraction $1/1$ (taken from Wikipedia). For this problem we append a fraction $0/0$ at the beginning of each series. So, the modified Farey sequences of order 1 to 8 are given below:

$$F_1 = \{0/0, 0/1, 1/1\}$$

$$F_2 = \{0/0, 0/1, 1/2, 1/1\}$$

$$F_3 = \{0/0, 0/1, 1/3, 1/2, 2/3, 1/1\}$$

$$F_4 = \{0/0, 0/1, 1/4, 1/3, 1/2, 2/3, 3/4, 1/1\}$$

$$F_5 = \{0/0, 0/1, 1/5, 1/4, 1/3, 2/5, 1/2, 3/5, 2/3, 3/4, 4/5, 1/1\}$$

$$F_6 = \{0/0, 0/1, 1/6, 1/5, 1/4, 1/3, 2/5, 1/2, 3/5, 2/3, 3/4, 4/5, 5/6, 1/1\}$$

$$F_7 = \{0/0, 0/1, 1/7, 1/6, 1/5, 1/4, 2/7, 1/3, 2/5, 3/7, 1/2, 4/7, 3/5, 2/3, 5/7, 3/4, 4/5, 5/6, 6/7, 1/1\}$$

$$F_8 = \{0/0, 0/1, 1/8, 1/7, 1/6, 1/5, 1/4, 2/7, 1/3, 3/8, 2/5, 3/7, 1/2, 4/7, 3/5, 5/8, 2/3, 5/7, 3/4, 4/5, 5/6, 6/7, 7/8, 1/1\}$$

Now we can represent each fraction p/q as a point (q, p) in the Cartesian plane. If we connect these points in the same order of Farey sequence (additionally the last one is connected to the first) we get a polygon. In this problem such a polygon will be called Farey Polygon of magnification 1. For example if we plot the fractions of F_4 in Cartesian plane and connect them in the same order as they are in the Farey sequence we get a Farey polygon of order four and magnification 1. This polygon is shown in Figure 1 (see the next page).

By multiplying the coordinates of vertices of Farey Polygon of order n , and magnification 1 with an integer m (and of course then connecting them) we get a Farey Polygon of order n and magnification m . For example in Figure 2 we see a Farey Polygon of order 4 and magnification 2. The number of lattice points inside this polygon is 5. Given the number of lattice points inside a lattice polygon, you will have to find its order and magnification.

Input

The input file contains **12000** lines of inputs. Each line contains a non-negative integer I , which denotes the number of lattice points inside the Farey Polygon. The value of I does not exceed 10^{16} . Input is terminated by a line containing **-1**. This line should not be processed.

Output

For each line of input produce one line of output. This line may contain two positive integers n and m that indicates the order and magnification respectively of the Farey Polygon, that has exactly I lattice points inside it. If there is more than one answer produce the one that has the minimum

positive n . If there is still a tie choose the minimum positive m . If no such Farey Polygon is found whose order and magnitude is less than **15001**, then print the line **"NOT FOUND"** (Without the quotes) instead.

Sample Input	Output for Sample Input
5	4 2
1	1 3
100	2 11
102	NOT FOUND
-1	

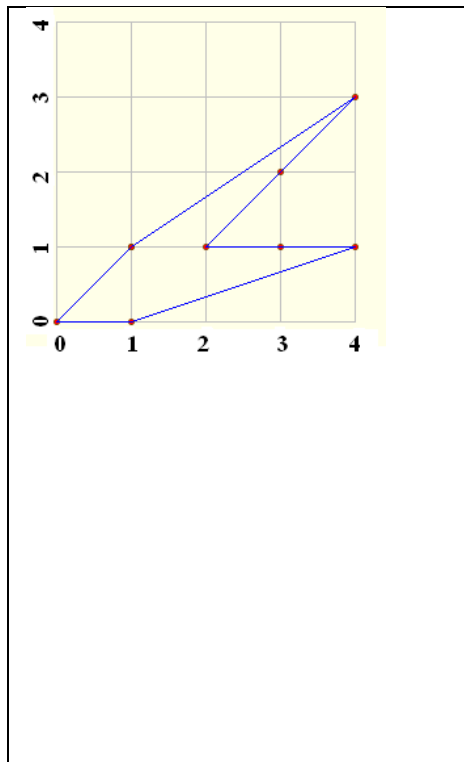


Figure 1: Farey Polygon of order 4 and magnification 1

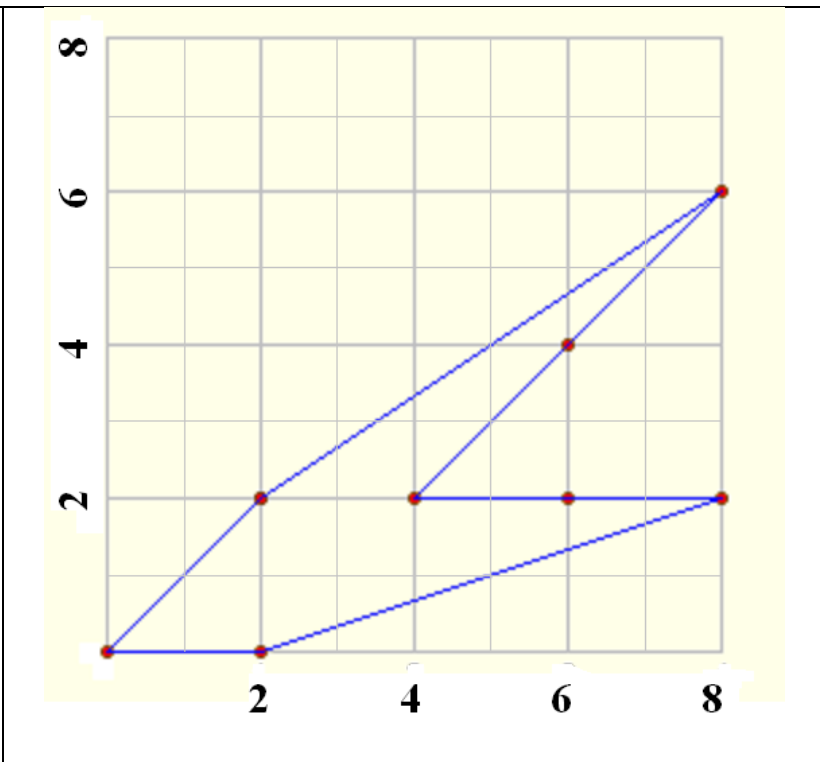


Figure 2: Farey Polygon of order 4 and magnification 2

Problem Setter: Shahriar Manzoor, Special Thanks: Derek Kisman