

B

Infinite Stable Integer

For any infinite-length decimal integer $S = d_1d_2d_3d_4\dots$ ($0 \leq d_i \leq 9, i \geq 1$), let $\text{prefix}(S,p)$ be the integer formed by the first p digits of S (i.e. $d_1d_2d_3\dots d_p$), and $F(S,i,p)$ be the percentage of digit i in $\text{prefix}(S,p)$. For example, if $S = 122312231223\dots$, $F(S,2,7) = \frac{4}{7} * 100$

We say S is stable if and only if every for digit i ($0 \leq i \leq 9$), there exists a real number $L(i)$ such that

$$\lim_{p \rightarrow \infty} F(S,i,p) = L(i)$$

Given three positive integers M, X and Y ($0 \leq X \leq Y < M$), and 10 pairs of integers $(A(0), B(0)), (A(1), B(1)), \dots, (A(9), B(9))$, find an infinite stable integer S such that:

1. Every $L(i)$ satisfies $A(i) \leq L(i) \leq B(i)$
2. For every integer $p \geq 1, X \leq (\text{prefix}(S,p) \bmod M) \leq Y$.

If there are more than one solution, maximize the average value of all the digits in S . Since S is stable, it can be proven that the average value converges.

For example, if $M=9, X=1$ and $Y=8, B(3)=B(4)=100$, all other $A(i)$ and $B(i)$ are zero, then the optimal S is $44(4444443)^*$, where $*$ means "repeated forever". It's not hard to see that $\text{prefix}(S,p)$ will never be a multiple of 9, and $L(3)=\frac{1}{7} * 100, L(4)=\frac{6}{7} * 100$, all other $L(i)=0$.

Input

There will be multiple test cases. Each test case contains 23 integers: $M, X, Y, A(0), A(1), \dots, A(9), B(0), B(1), \dots, B(9)$. $2 \leq M \leq 50, 0 \leq X \leq Y < M, 0 \leq A(i) \leq B(i) \leq 100$.

Output

For each test case, print case number and the maximal average value rounded to 8 decimal places. If no infinite stable integer can be found, print "NO SOLUTION" instead. Look at the output for sample input for details.

Sample Input																						
2	1	1	0	0	0	0	0	0	0	0	0	0	0	20	20	20	20	20	20	20	20	20
9	1	8	0	0	0	0	0	0	0	0	0	0	0	0	0	0	100	100	0	0	0	0
8	0	7	1	1	1	1	1	1	1	1	1	1	1	2	2	2	2	2	2	2	2	2
19	2	3	0	0	0	0	0	0	0	0	0	0	0	100	100	100	100	100	100	100	100	100
Output for Sample Input																						
Case 1: 5.00000000																						
Case 2: 3.85714286																						
Case 3: NO SOLUTION																						
Case 4: 1.00000000																						