

## Problem D

### DNA Subsequences

*Source file name:* `sequence.c`, `sequence.cpp` *or* `sequence.java`

Thomas, a computer scientist that works with DNA sequences, needs to compute longest common subsequences of given pairs of strings. Consider an alphabet  $\Sigma$  of letters and a word  $w = a_1a_2 \cdots a_r$ , where  $a_i \in \Sigma$ , for  $i = 1, 2, \dots, r$ . A **subsequence** of  $w$  is a word  $x = a_{i_1}a_{i_2} \cdots a_{i_s}$  such that  $1 \leq i_1 < i_2 < \dots < i_s \leq r$ . Subsequence  $x$  is a **segment** of  $w$  if  $i_{j+1} = i_j + 1$ , for  $j = 1, 2, \dots, s - 1$ . For example the word `ove` is a segment of the word `lovely`, whereas the word `loly` is a subsequence of `lovely`, but not a segment.

A word is a **common subsequence** of two words  $w_1$  and  $w_2$  if it is a subsequence of each of the two words. A **longest common subsequence** of  $w_1$  and  $w_2$  is a common subsequence of  $w_1$  and  $w_2$  having the largest possible length. For example, consider the words  $w_1 = \text{lovxxelyxxxxx}$  and  $w_2 = \text{xxxxxxlovely}$ . The words  $w_3 = \text{lovely}$  and  $w_4 = \text{xxxxxxx}$ , the latter of length 7, are both common subsequences of  $w_1$  and  $w_2$ . In fact,  $w_4$  is their longest common subsequence. Notice that the empty word, of length zero, is always a common subsequence, although not necessarily the longest.

In the case of Thomas, there is an extra requirement: the subsequence must be formed from common segments having length  $K$  or more. For example, if Thomas decides that  $K = 3$ , then he considers `lovely` to be an acceptable common subsequence of `lovxxelyxxxxx` and `xxxxxxlovely`, whereas `xxxxxxx`, which has length 7 and is also a common subsequence, is not acceptable. Can you help Thomas?

### Input

The input contains several test cases. The first line of a test case contains an integer  $K$  representing the minimum length of common segments, where  $1 \leq K \leq 100$ . The next two lines contain each a string on lowercase letters from the regular alphabet of 26 letters. The length  $\ell$  of each string satisfies the inequality  $1 \leq \ell \leq 10^3$ . There are no spaces on any line in the input. The end of the input is indicated by a line containing a zero.

*The input must be read from standard input.*

### Output

For each test case in the input, your program must print a single line, containing the length of the longest subsequence formed by consecutive segments of length at least  $K$  from both strings. If no such common subsequence of length greater than zero exists, then 0 must be printed.

*The output must be written to standard output.*

Sample input	Output for the sample input
3 lovxxelyxxxxx xxxxxxxlovely	6 7 10
1 lovxxelyxxxxx xxxxxxxlovely	0
3 lovxxxelxyxxxx xxxlovelyxxxxxxxx	
4 lovxxxelyxxx xxxxxxxlovely	
0	